

系組：資訊科學系三年級 日期節次：7 月 30 日第 3 節 13:30-14:50

科目：離散數學 (124-139)

單選題 無倒扣 每題 5 分

1. What is fundamental theorem of arithmetic?

(A) A positive integer n greater than 1 is composite if and only if n has a divisor d

satisfying $2 \leq d \leq \sqrt{n}$

(B) Any integer greater than 1 can be written as a product of primes.

(C) The number of primes is infinite

(D) For any positive integers m and n , $\gcd(m,n) * \text{lcm}(m,n) = mn$

2. Compute the hexadecimal number $4A+B4$

(A) FE

(B) EF

(C) EE

(D) FG

3. How many mod operations are there when using Euclidean algorithm to find $\gcd(504,306)$, mod is modulus operation.

(A) 5

(B) 7

(C) 4

(D) 3

4. How many mod operations are there when using Euclidean algorithm to find $\gcd(273,110)$

(A) 5

(B) 7

(C) 4

(D) 3

5. p and q are primes. $z=pq$. $\phi = (p-1)(q-1)$, $0 \leq a \leq z-1$, The security of RSA rest primarily on

- (A) The number of primes is infinite
- (B) $a^u \bmod z = a$ for all $0 \leq a < z$ and $u \bmod \phi = 1$
- (C) the inability of knowing z to discover p and q
- (D) none of the above

6. (Pigeonhole principle) Let f be a function from a finite set X into a finite set Y . Suppose that $|X|=n$ and $|Y|=m$. Then there are at least k values $a_1, a_2, \dots, a_k \in X$ such that

$$f(a_1) = f(a_2) = \dots = f(a_k)$$

- (A) $k = \lceil n/m \rceil$
- (B) $k = \lfloor m/n \rfloor$
- (C) $k = \lceil n/(m+1) \rceil$
- (D) $k = \lfloor m/(n+1) \rfloor$

7. Convert the decimal number 456 to octal

- (A) 710
- (B) 701
- (C) 720
- (D) 702

8. $a_n = 6a_{n-1} - 8a_{n-2}$, $a_0 = 1, a_1 = 0$, the solution is $a_n = x^{n+1} - y^n$, $x+y=?$

- (A) 3
- (B) 4
- (C) 5
- (D) 6

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9. $2a_n = 7a_{n-1} - 3a_{n-2}, a_0 = 1, a_1 = 1$, the solution is $a_n = (x^{2-n} + y^n)/z, x+y+z=?$

- (A) 8
- (B) 9
- (C) 10
- (D) 11

10. $a_n = -8a_{n-1} - 16a_{n-2}, a_0 = 2, a_1 = -20$, the solution is $a_n = x(-4)^n + yn(-4)^n, x+y=?$

- (A) 3
- (B) 4
- (C) 5
- (D) 6

11. $a_n = -3a_{n-1}, a_0 = 2$, the solution is $a_n = x(y)^n, x+y=?$

- (A) -3
- (B) -1
- (C) 2
- (D) 4

12. Which one is wrong?

- (A) The worst case time for binary search for input size n is $\Theta(\lg n)$
- (B) The best, average and worst time are different for selection sort.
- (C) The worst case time for merge sort for input size n is $\Theta(n \lg n)$
- (D) The worst time for selection sort is $O(n^2)$.

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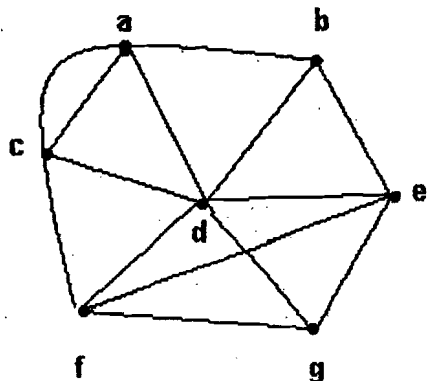
13.

Program	# of lines	# of "return"	# of function calls
1	66	20	1
2	41	10	2
3	68	5	8
4	90	34	5
5	75	12	14

Construct the dissimilarity using city block distance. If the threshold is set as 19, then the final classes are?

- (A) $\{1,3,5\}, \{2\}, \{4\}$
- (B) $\{1,3\}, \{5\}, \{2,4\}$
- (C) $\{1\}, \{2\}, \{3\}, \{4\}, \{5\}$
- (D) $\{1,3,5\}, \{2,4\}$

14. The total degrees of the following graph is



- (A) 22
- (B) 24
- (C) 26
- (D) 28

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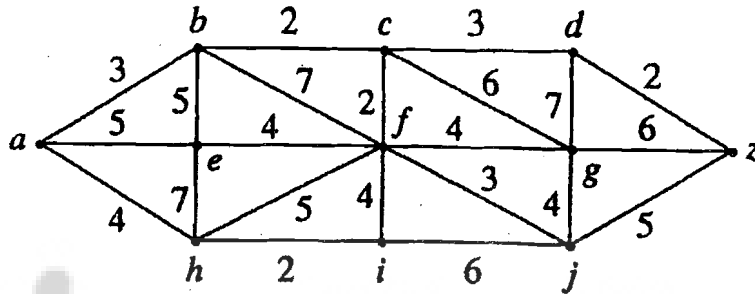
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15. The length of the shortest path from a to z is x and the length of the shortest path from h to d is y . $x+y=?$



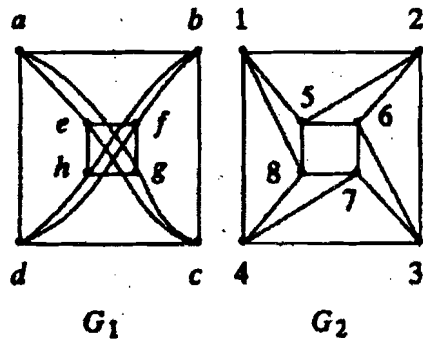
(A) 19

(B) 20

(C) 26

(D) 29

16. which one is right?



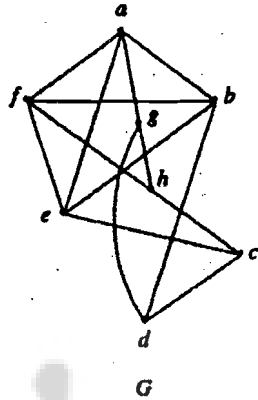
(A) G_1 and G_2 are isomorphic

(B) G_1 and G_2 are not isomorphic because some vertex degrees are different

(C) G_1 and G_2 are not isomorphic because number of edges are different

(D) G_1 and G_2 are not isomorphic because the length of simple cycle is invariant

17. which one is right?



- (A) G is a planar graph
- (B) G is not a planar graph because G contains a subgraph homeomorphic to K_5
- (C) G is not a planar graph because G contains a subgraph homeomorphic to $K_{3,3}$
- (D) G has e edges, v vertices and faces f and $f = e - v + 2$

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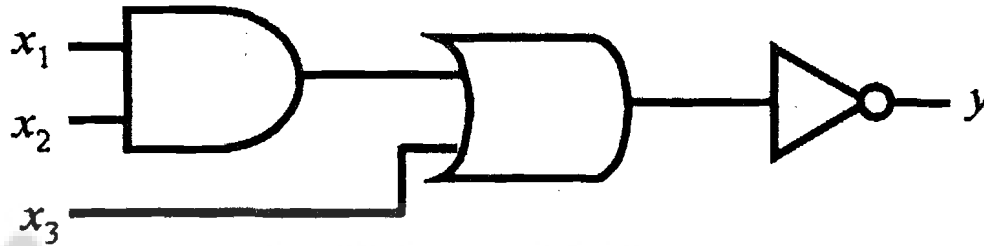
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18.



the corresponding logic table is

x_1	x_2	x_3	y
1	1	1	a
1	1	0	b
1	0	1	c
1	0	0	d
0	1	1	e
0	1	0	f
0	0	1	g
0	0	0	h

Transform the binary "abcdefgh" to decimal.

- (A) 21
- (B) 22
- (C) 20
- (D) 10

19. \oplus is exclusive OR

x1	x2	$x1 \oplus x2$
1	1	a
1	0	b
0	1	c
0	0	d

Transform the binary "abcd" to decimal.

- (A) 1
- (B) 6
- (C) 4
- (D) 10

20. Find the disjunctive normal form of f.

x	y	z	$f(x, y, z)$
1	1	1	1
1	1	0	0
1	0	1	0
1	0	0	1
0	1	1	0
0	1	0	0
0	0	1	0
0	0	0	1

- (A) $xyz \vee x\bar{y}\bar{z} \vee \bar{x}y\bar{z}$
- (B) $\bar{x}yz \vee x\bar{y}z \vee \bar{x}y\bar{z}$
- (C) $xy\bar{z} \vee x\bar{y}z \vee \bar{x}y\bar{z}$
- (D) $xyz \vee x\bar{y}z \vee xy\bar{z}$

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